

# Observations of the Sun's Meridional Flow

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With special thanks to:

Michael J. Thompson  
University of Sheffield

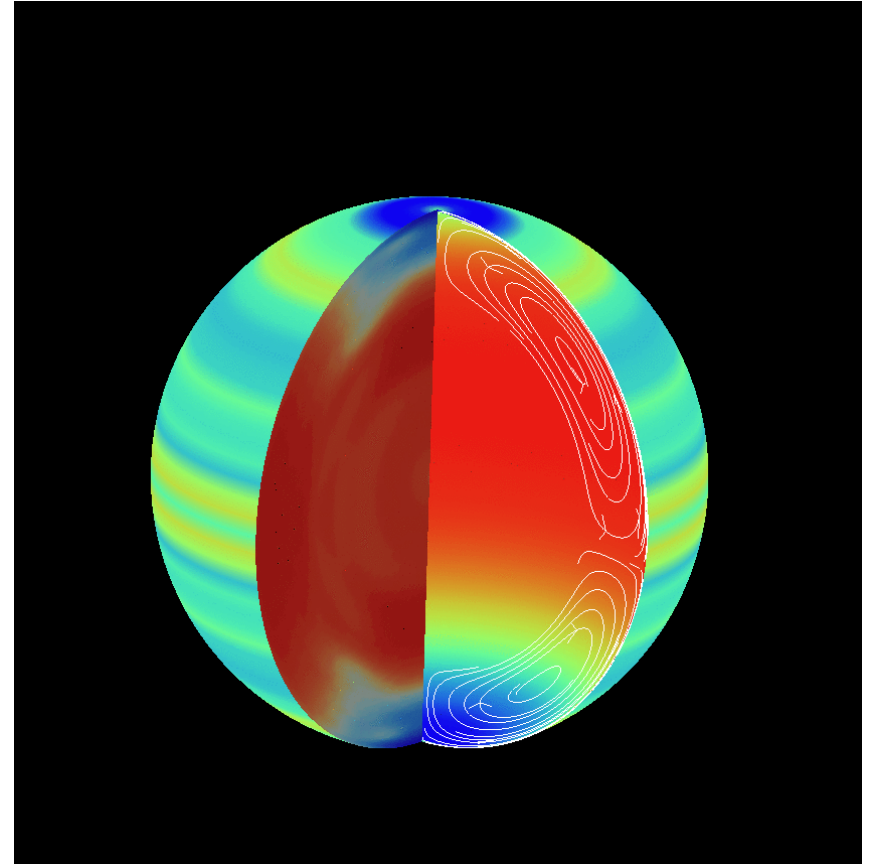
Sasha Kosovichev & SOHO/MDI team  
Stanford University

# Overview

- Introduction, Motivation
- Data set-up and analysis
- Radial meridional flow profile of the quiet Sun
- Variations with the solar cycle
- Conclusions

# The meridional flow

- First meridional flow measurements at the solar surface were made in the late 1970's
  - Duvall (1979), Howard (1979), Beckers & Taylor (1980)
- Poleward flow of around 15 – 20 m/s
- Conservation of mass: flow needs to return equatorward at some depth



# Comparison of flow velocities

- Differential Rotation at surface
  - $0^\circ$  :  $P=25$  days;  $v=2000$  m/s
  - $45^\circ$ :  $P=27$  days;  $v=1300$  m/s
  - $60^\circ$ :  $P=28$  days;  $v=900$  m/s
- Meridional Flow
  - At surface  $v \approx 20$  m/s poleward
  - Predicted at base of convection zone
  - $v \approx 1 - 3$  m/s

# Why are we interested?

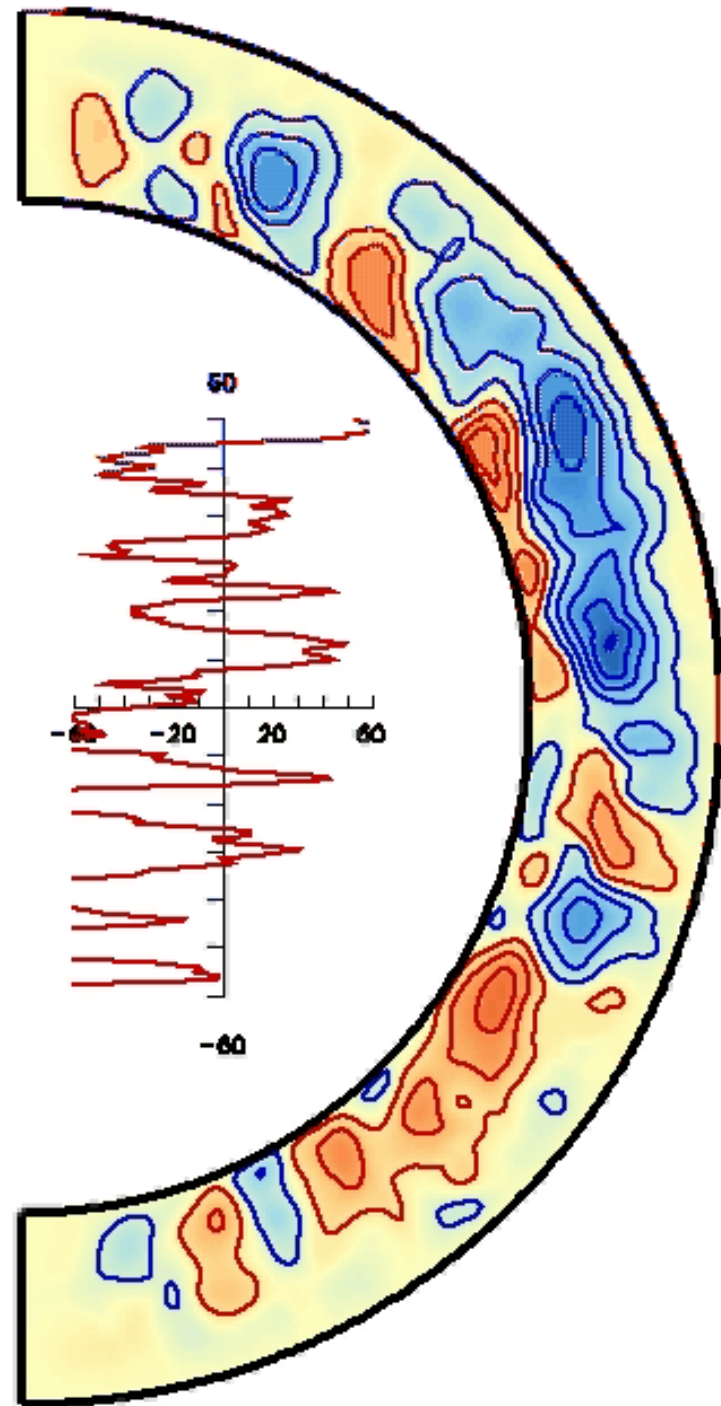
- The radial meridional flow profile would give strong constraints to many theories of the solar interior and dynamo models
- Mean-field models of angular momentum transport (e.g. Gilman 1972, Rüdiger 1989; reviews by Thompson et al. 2003, Miesch 2005, Shibahashi 2007)
  - Establish and maintain differential rotation
  - Balance of differential rotation, Reynolds' stresses and meridional circulation (and magnetic field, and viscosity, etc.)
- Flux-transport models of solar dynamo (Babcock-Leighton models) (e.g. Wang et al. 1991, Dikpati & Charbonneau 1999)
  - Transport surface poloidal magnetic field to bottom of convection zone, where it can then be converted into toroidal magnetic field by rotational shear

# Open Questions

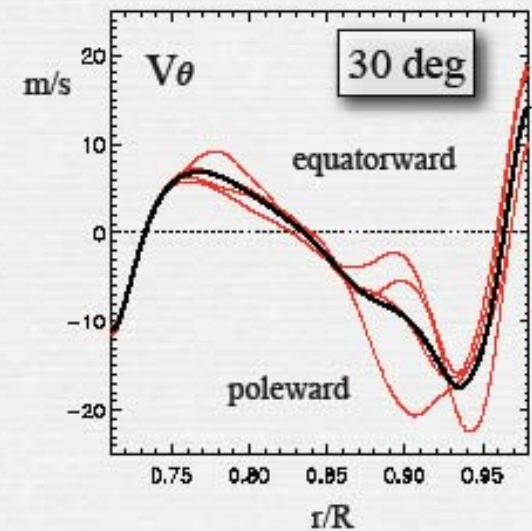
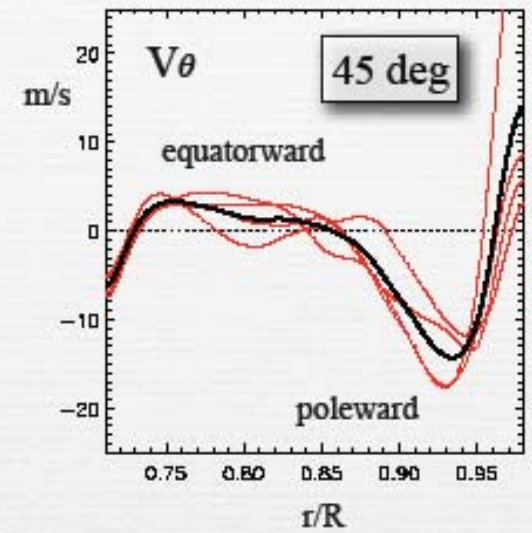
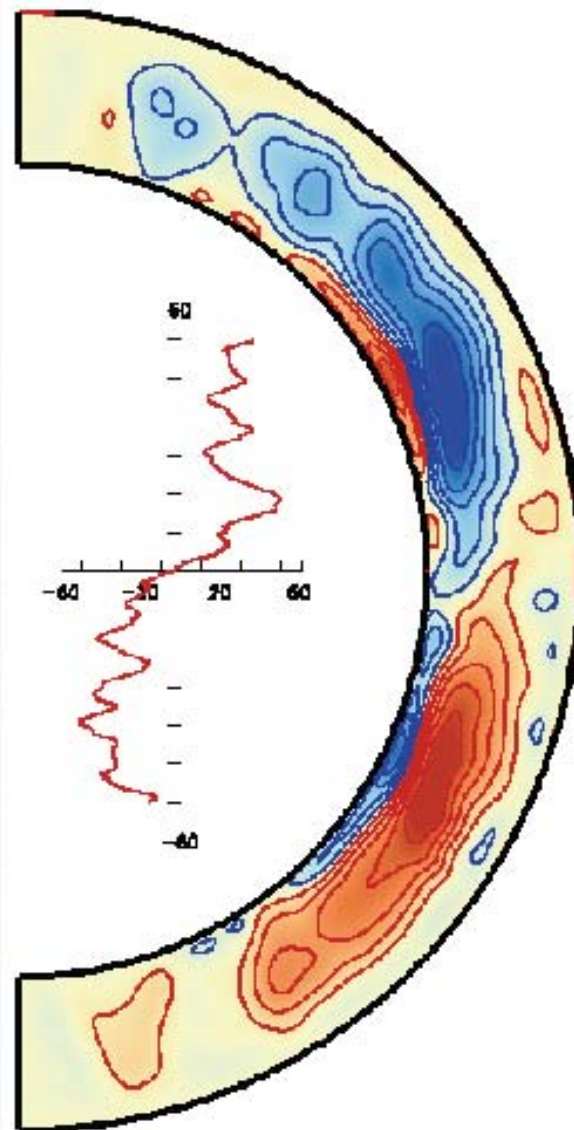
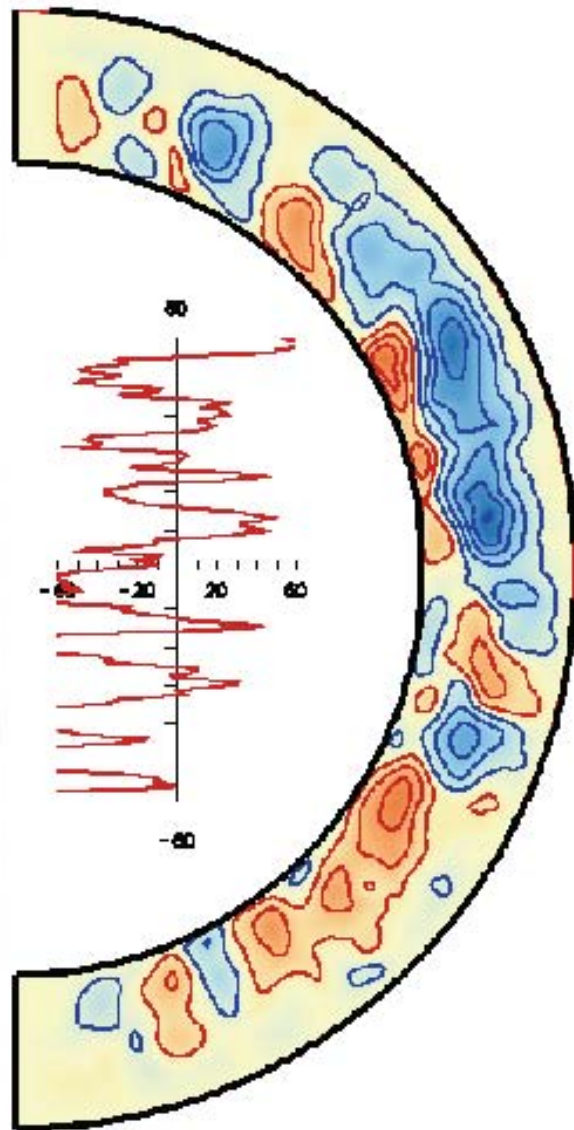
- Is the meridional circulation contained within the convection zone?
- Is the equatorward return flow above or below the tachocline?
- Is there a single, or are there multiple meridional cells?
- How does the meridional flow vary with the solar cycle?

Numerical simulation  
of meridional  
circulation  
  
using turbulent  
convection model

Courtesy of Mark Miesch



# Variability of Meridional Circulation

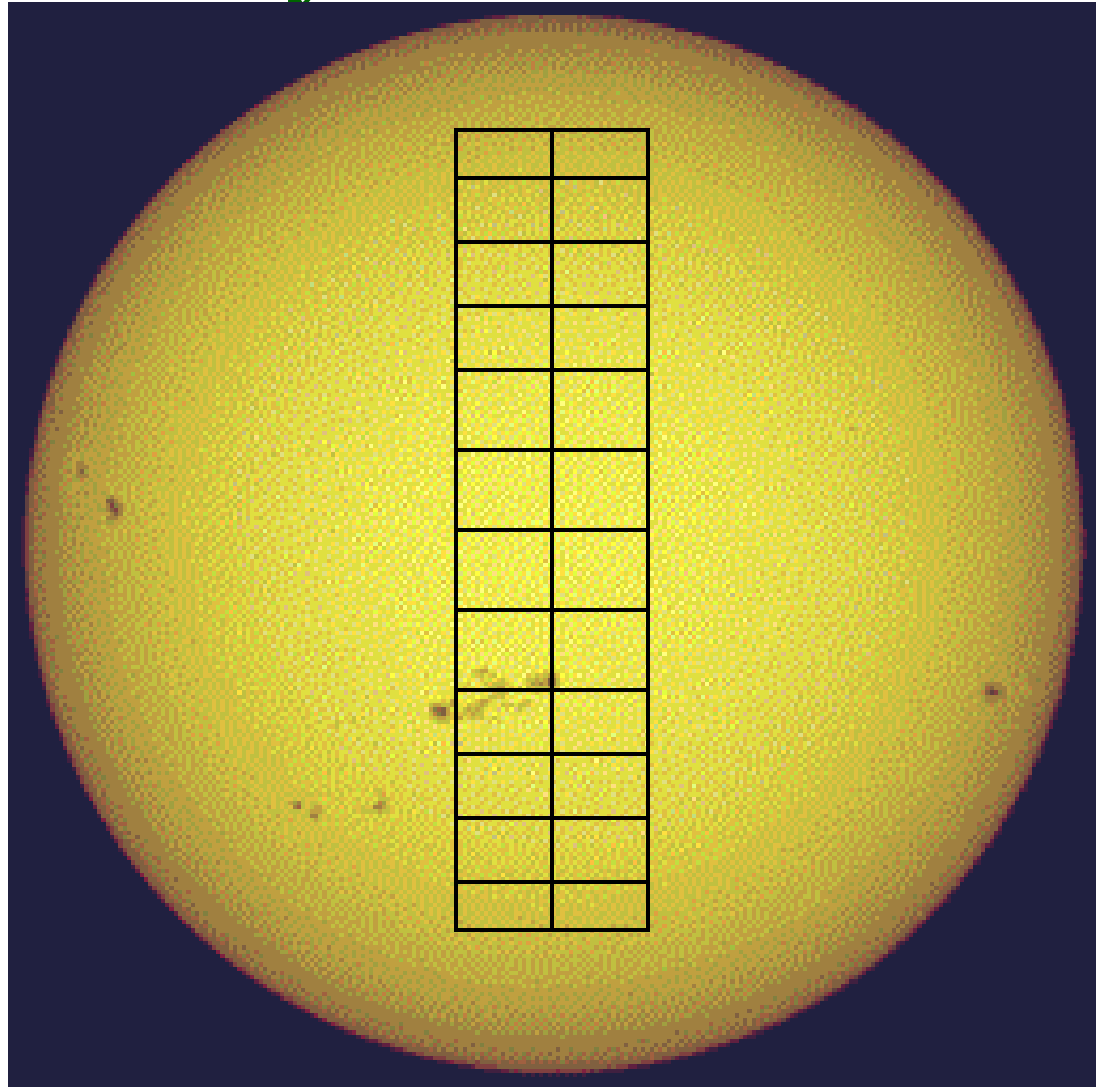




# Data Layout

Large FOV to probe deep → SOHO/MDI data

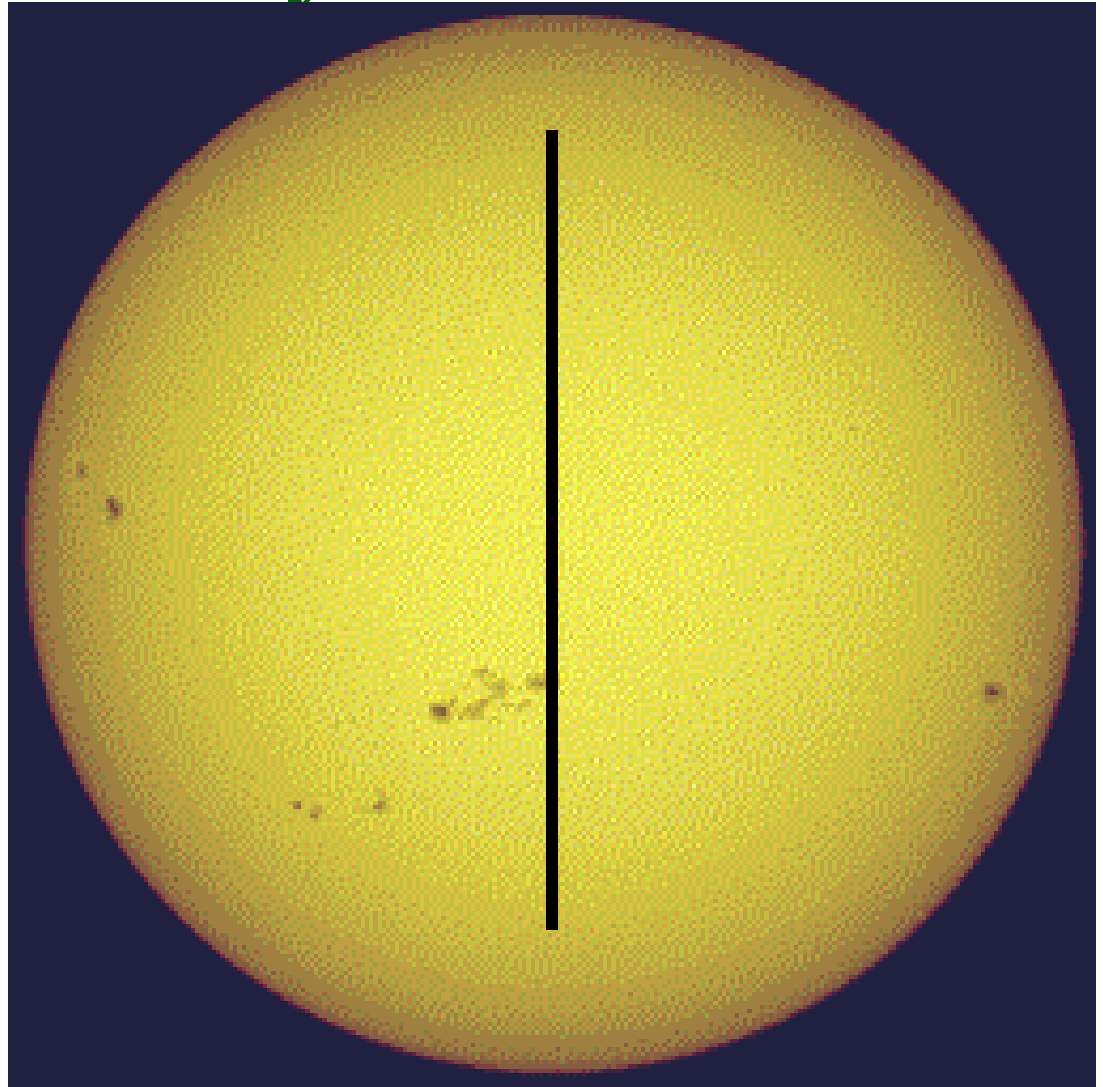
SOHO/MDI tracked velocity data along the Center Meridian



# Data Layout

Set-up: 1+1D along  
center meridian

Merge data to form  
a spatially  
1dimensional grid in  
North-South  
direction, evenly  
spaced in latitude



# Data Layout

Signal:  $f(t, \theta)$

Power spectrum:

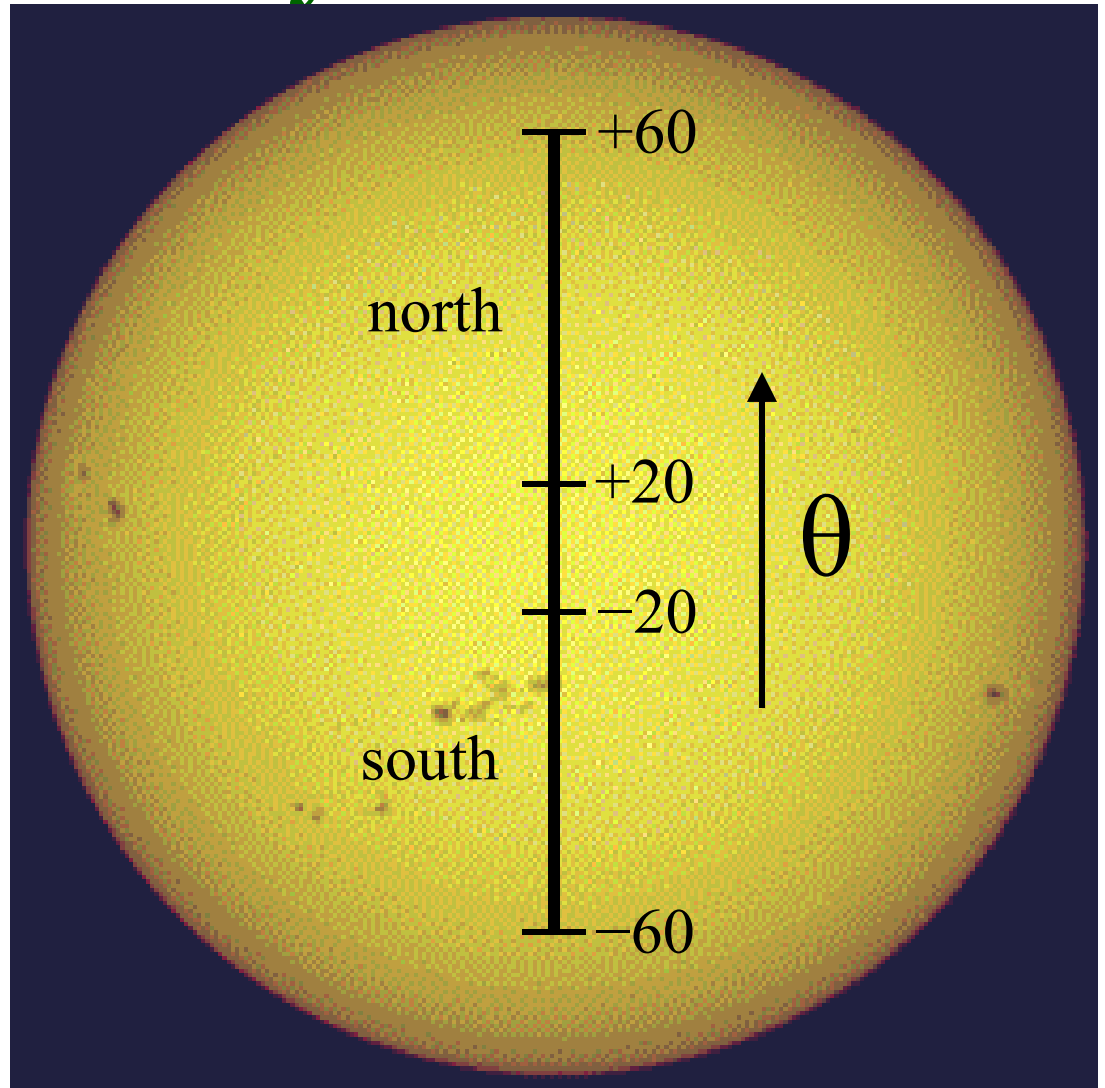
$$P(\omega, k_\theta) = |\hat{f}(\omega, k_\theta)|^2$$

with  $\omega = 2\pi\nu$

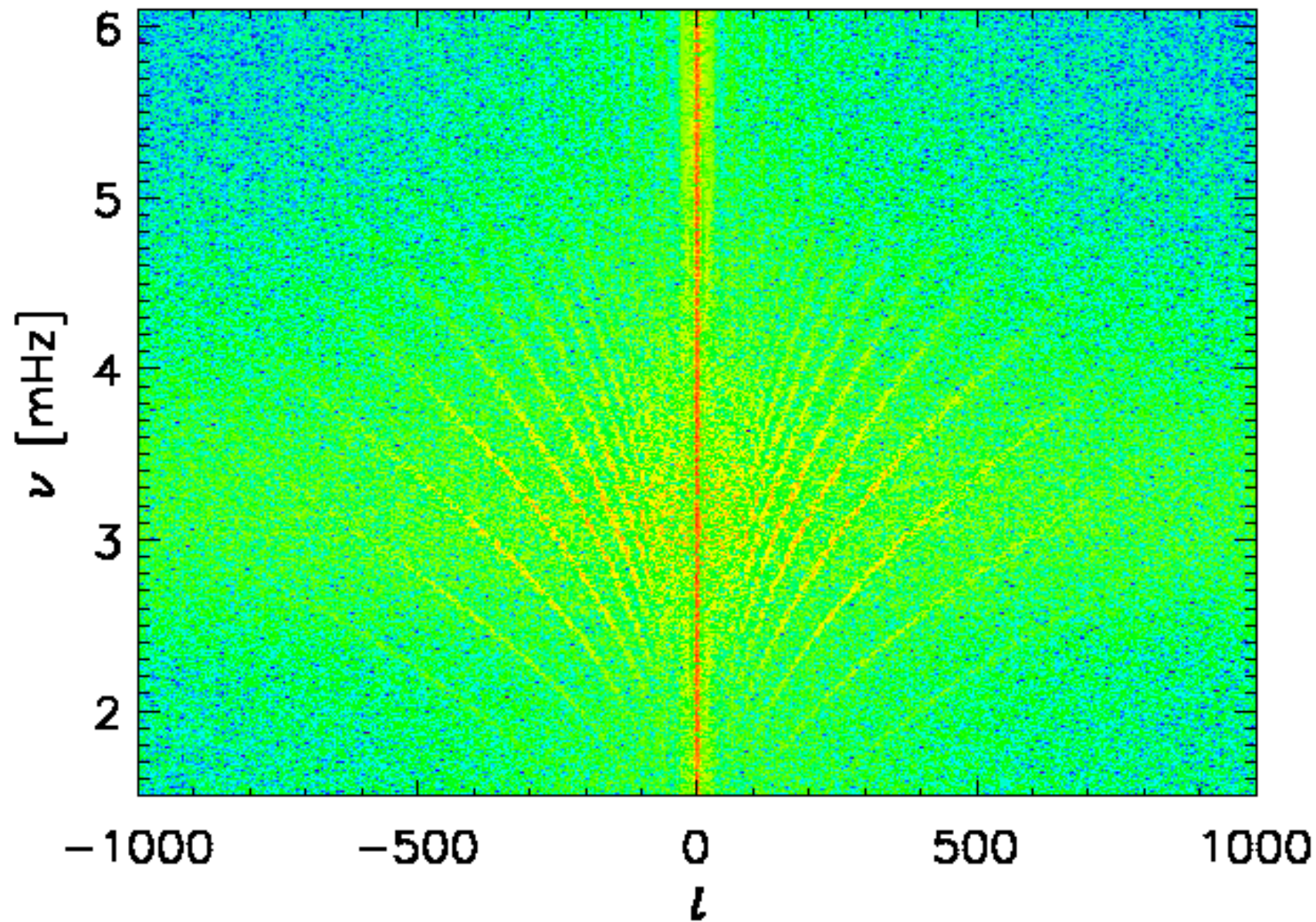
and  $k_\theta \hat{=} l$

we get the power spectrum as a function of  $\nu$  and  $l$ :

$$P(\nu, l)$$

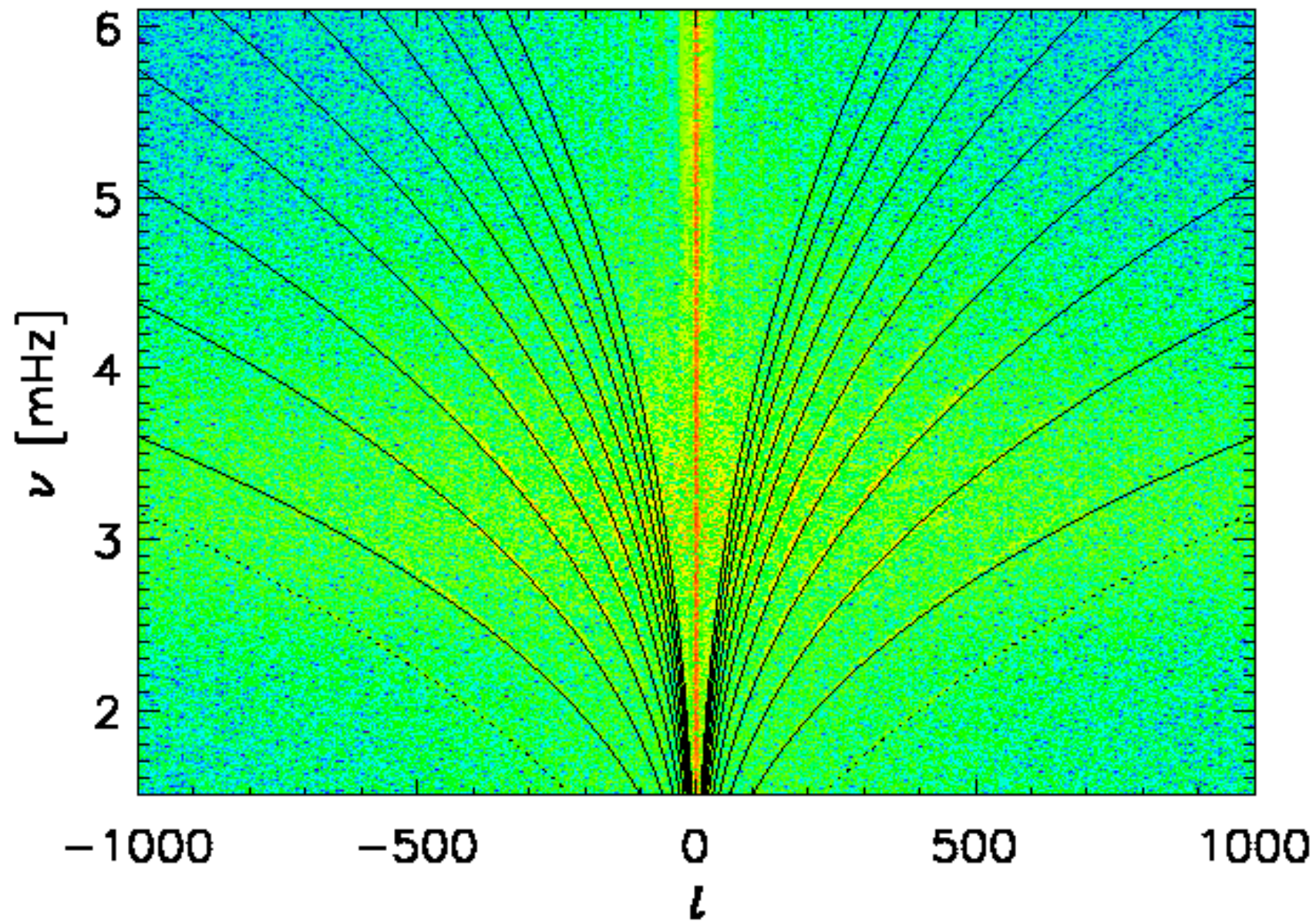


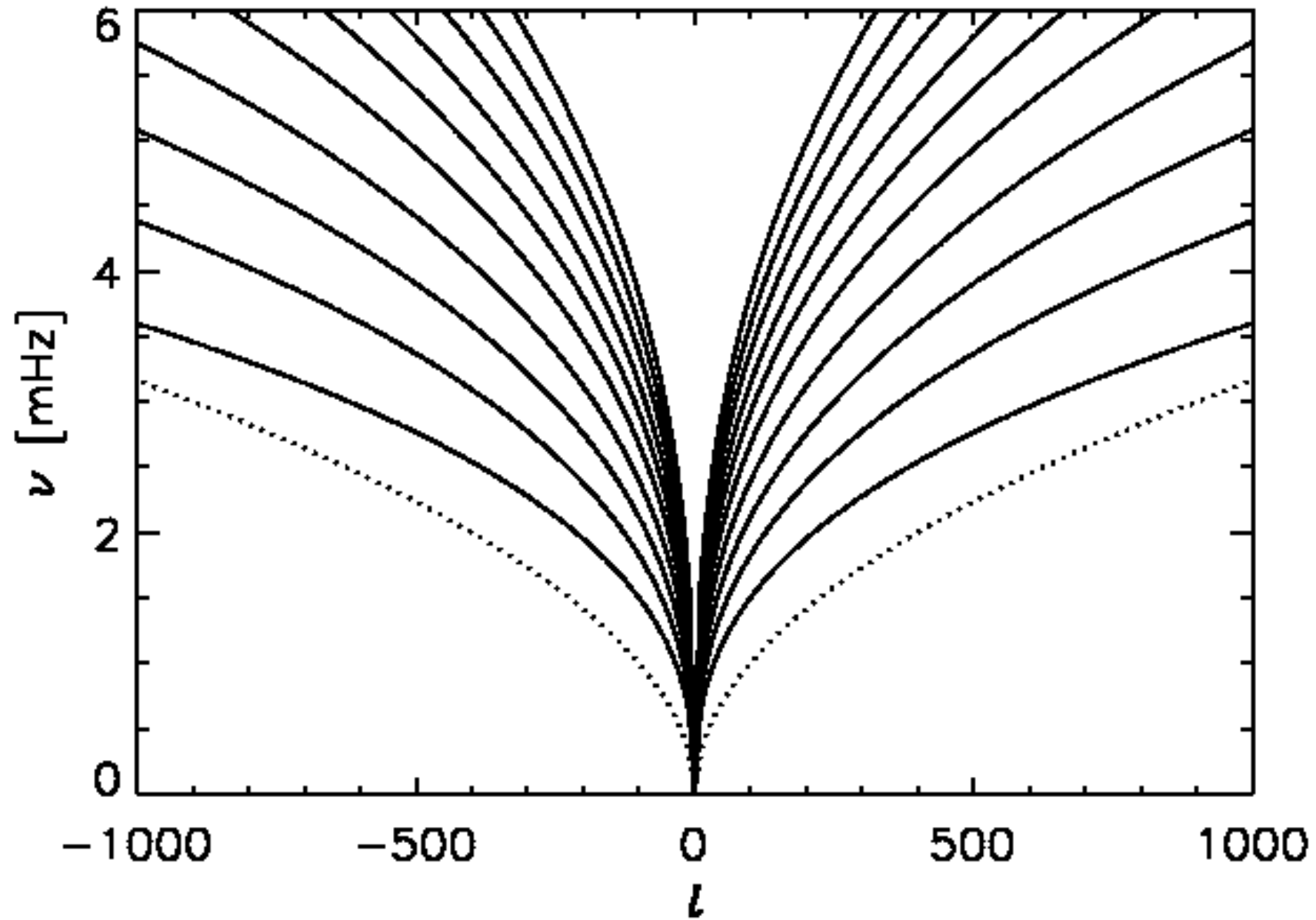
CR 1922, lat: +20...+60

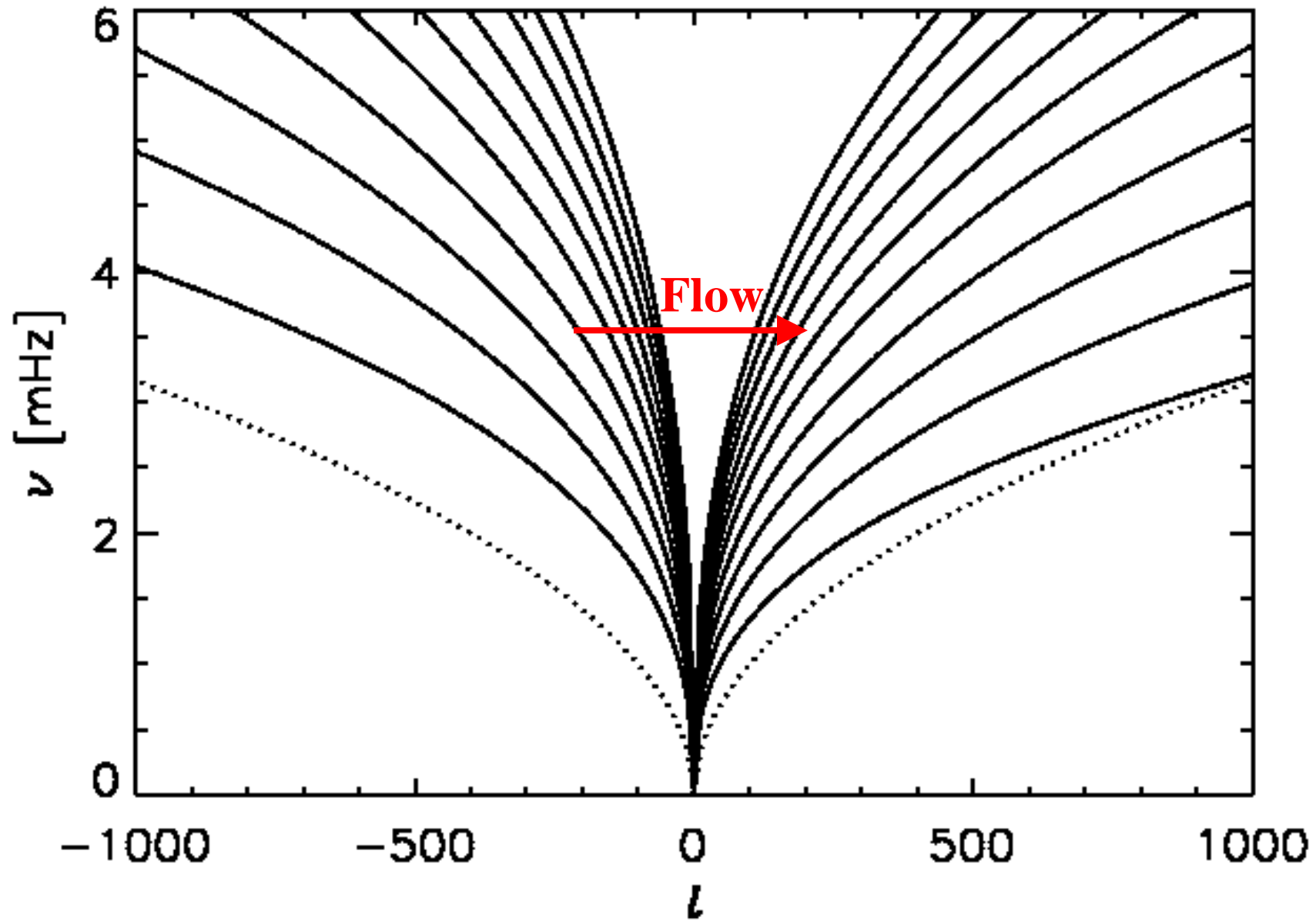




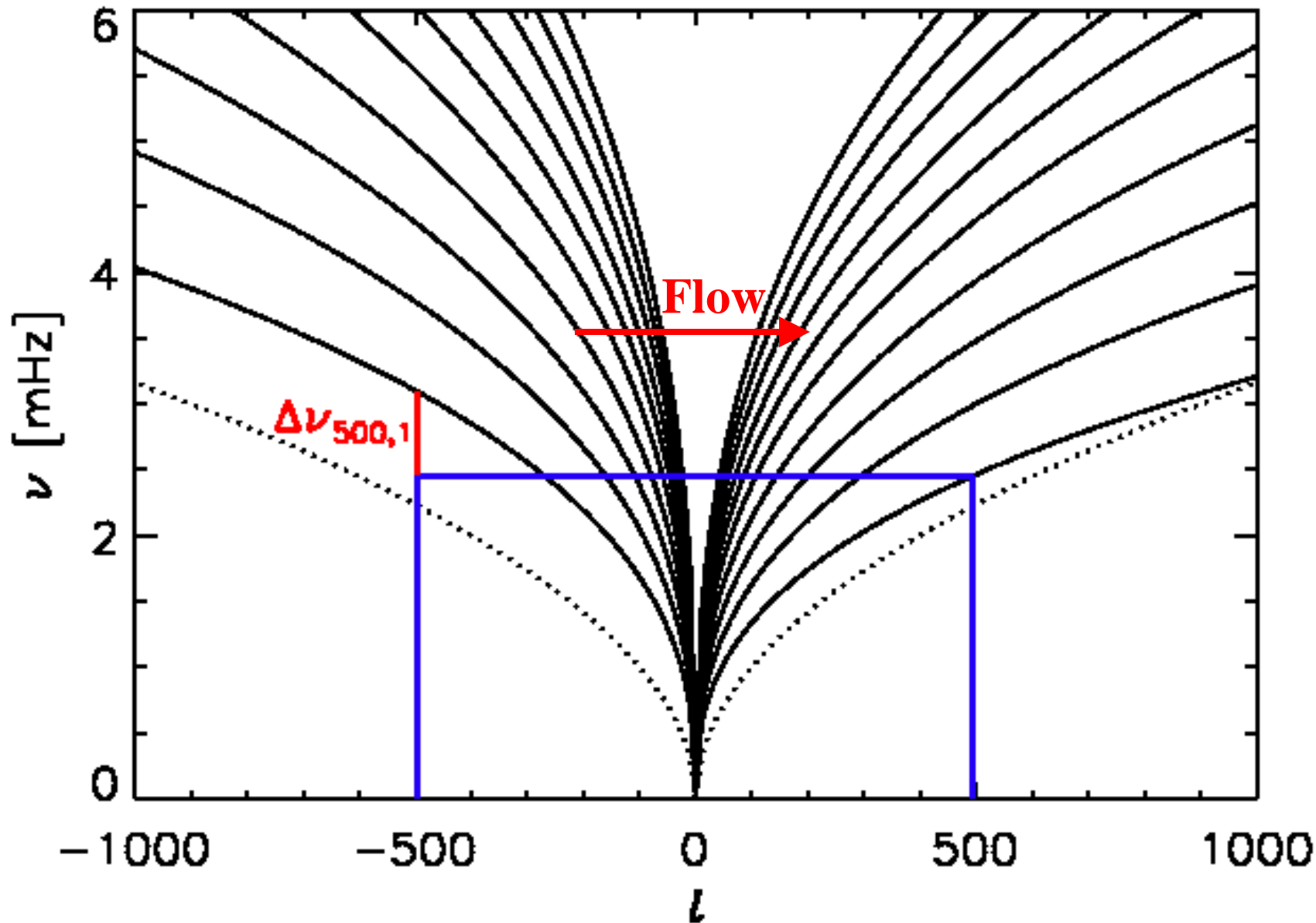
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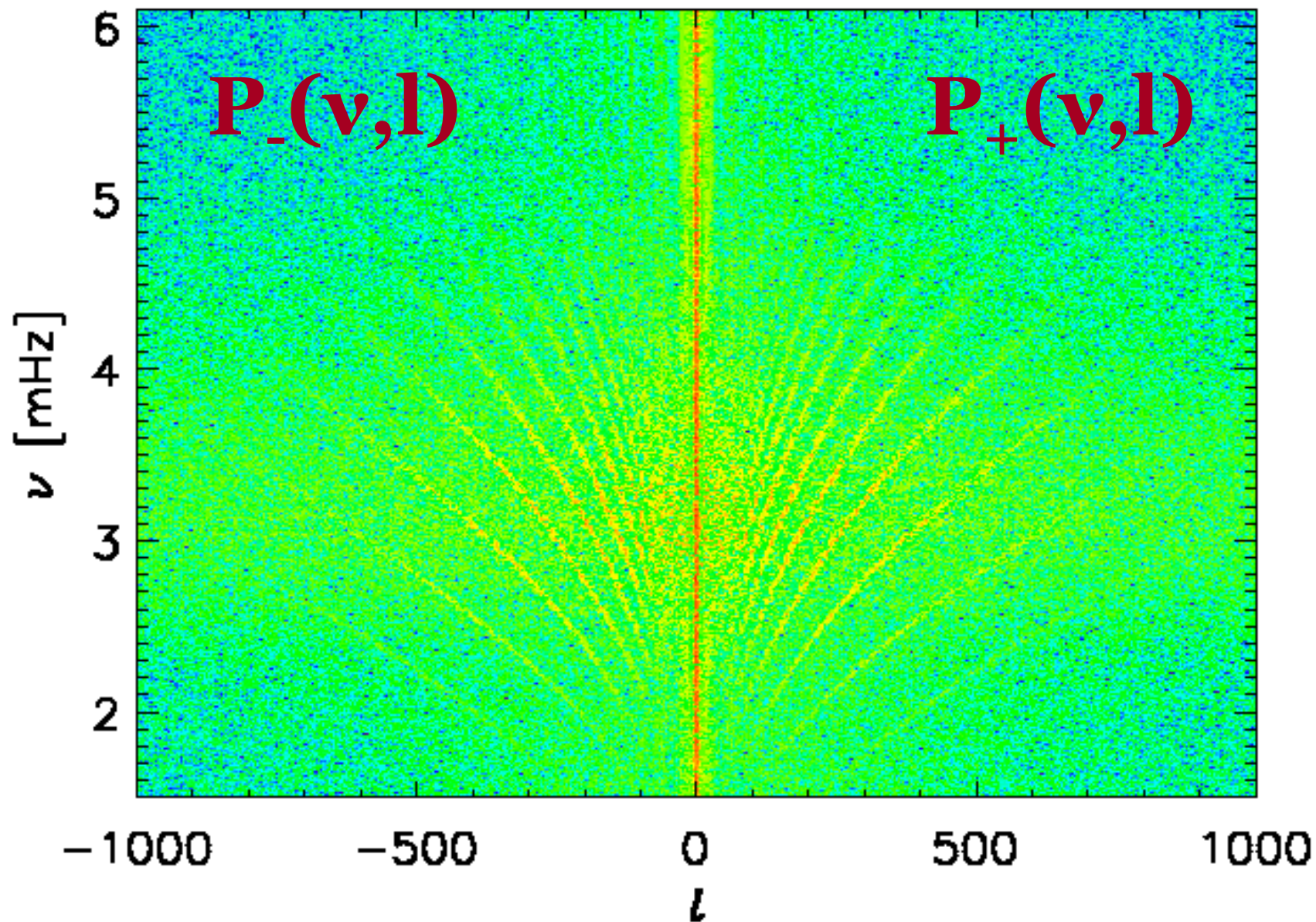


$$\text{Flow } U'(v/l) = \Delta v_{lp} \pi R_{\text{sun}} / l$$

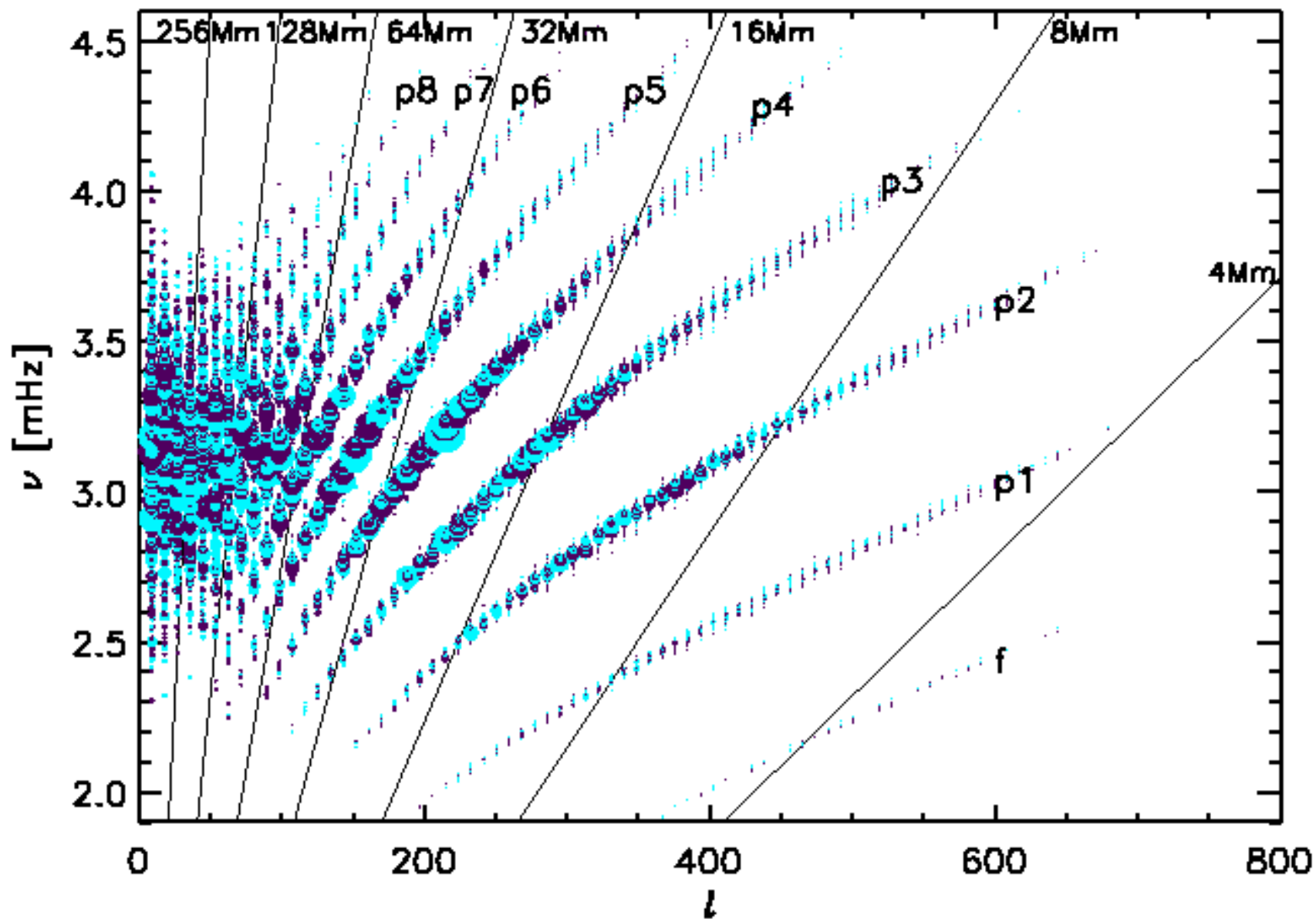




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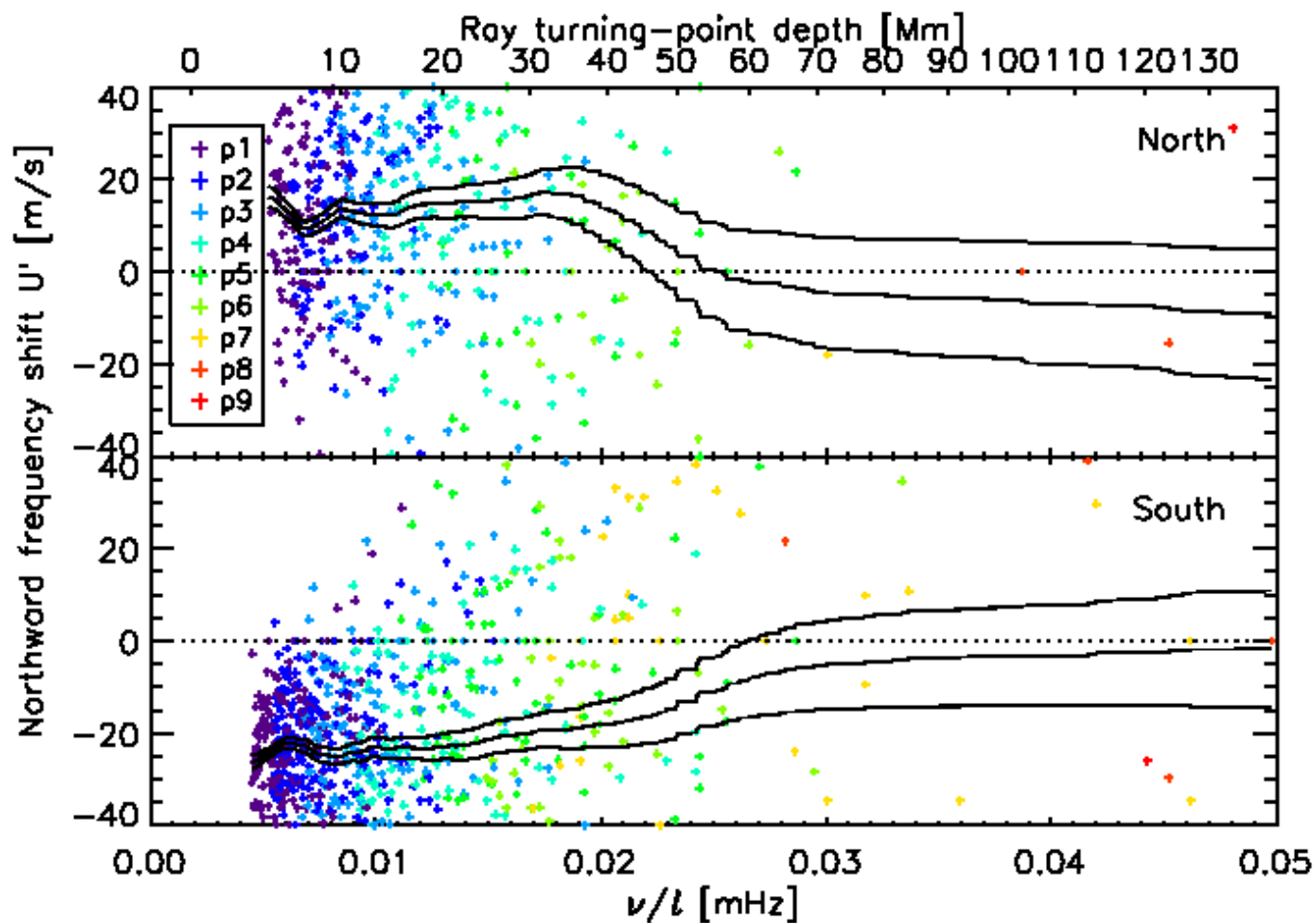


$$P_+(\nu, l) - P_-(\nu, l)$$

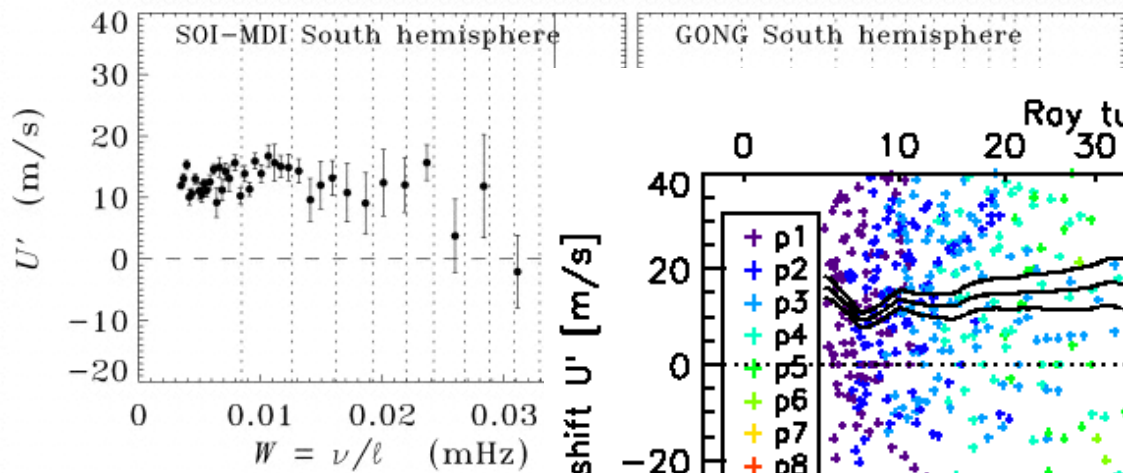
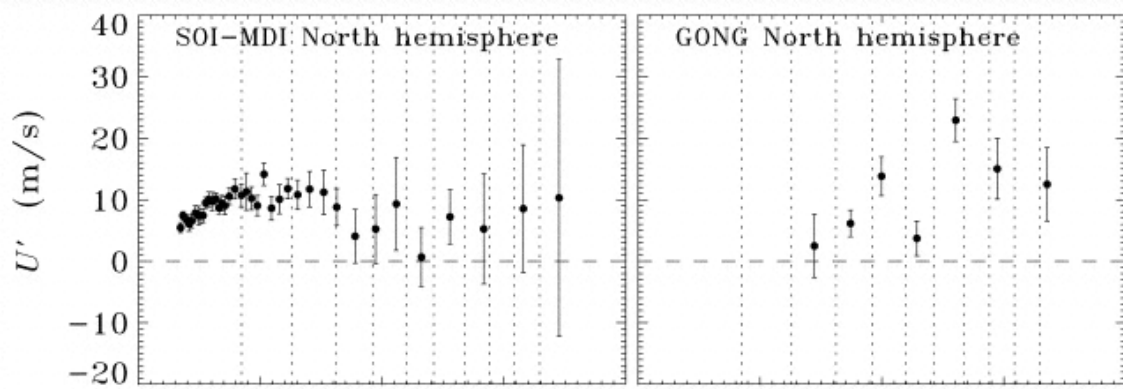


# Average 80 days frequency shift during solar min

Mitra-Kraev & Thompson (2007) AN 328 1009



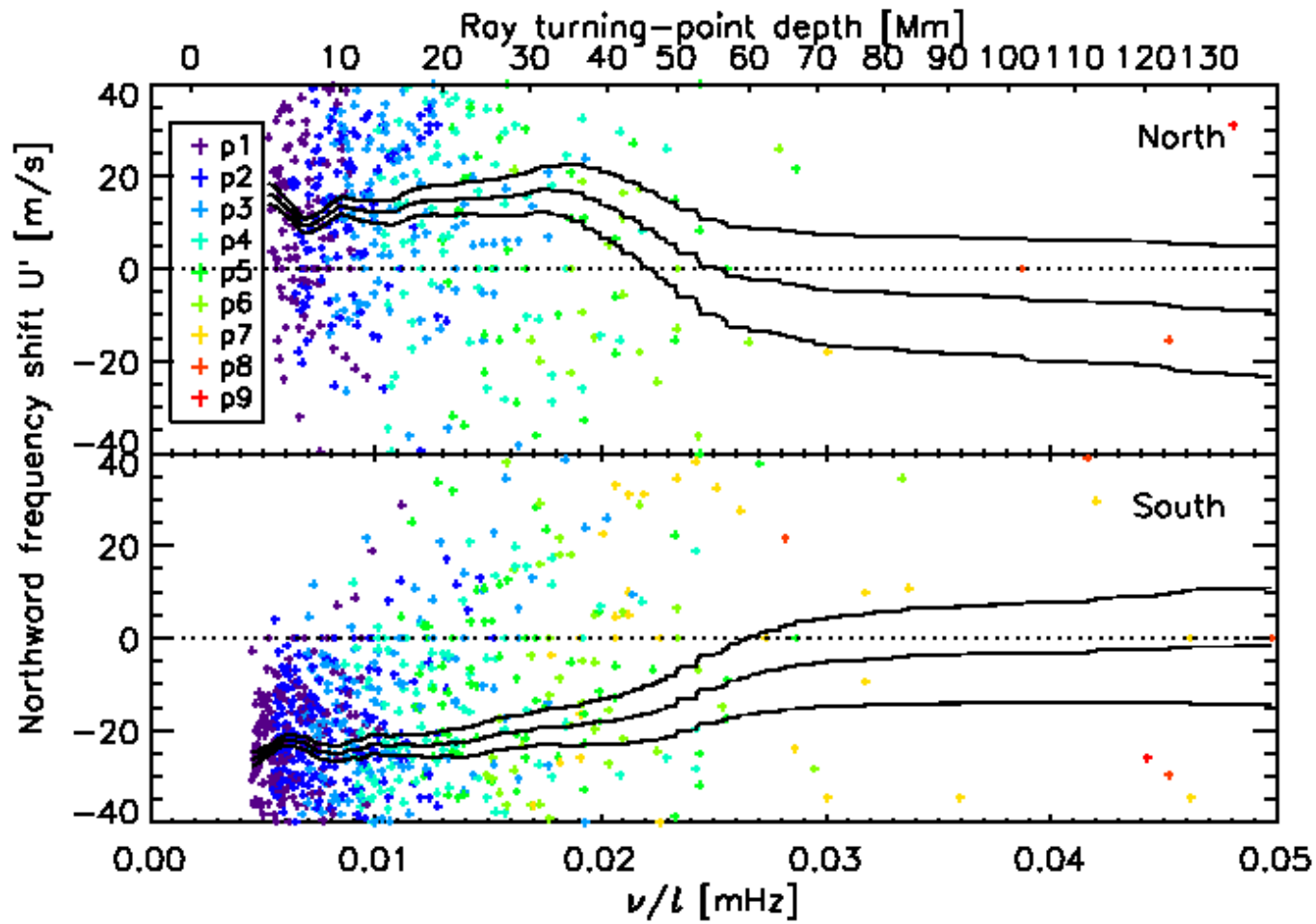




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ra-Kraev & Thompson (2007) AN 328 1009

Braun & Fan (1998)  
ApJ 508 L105



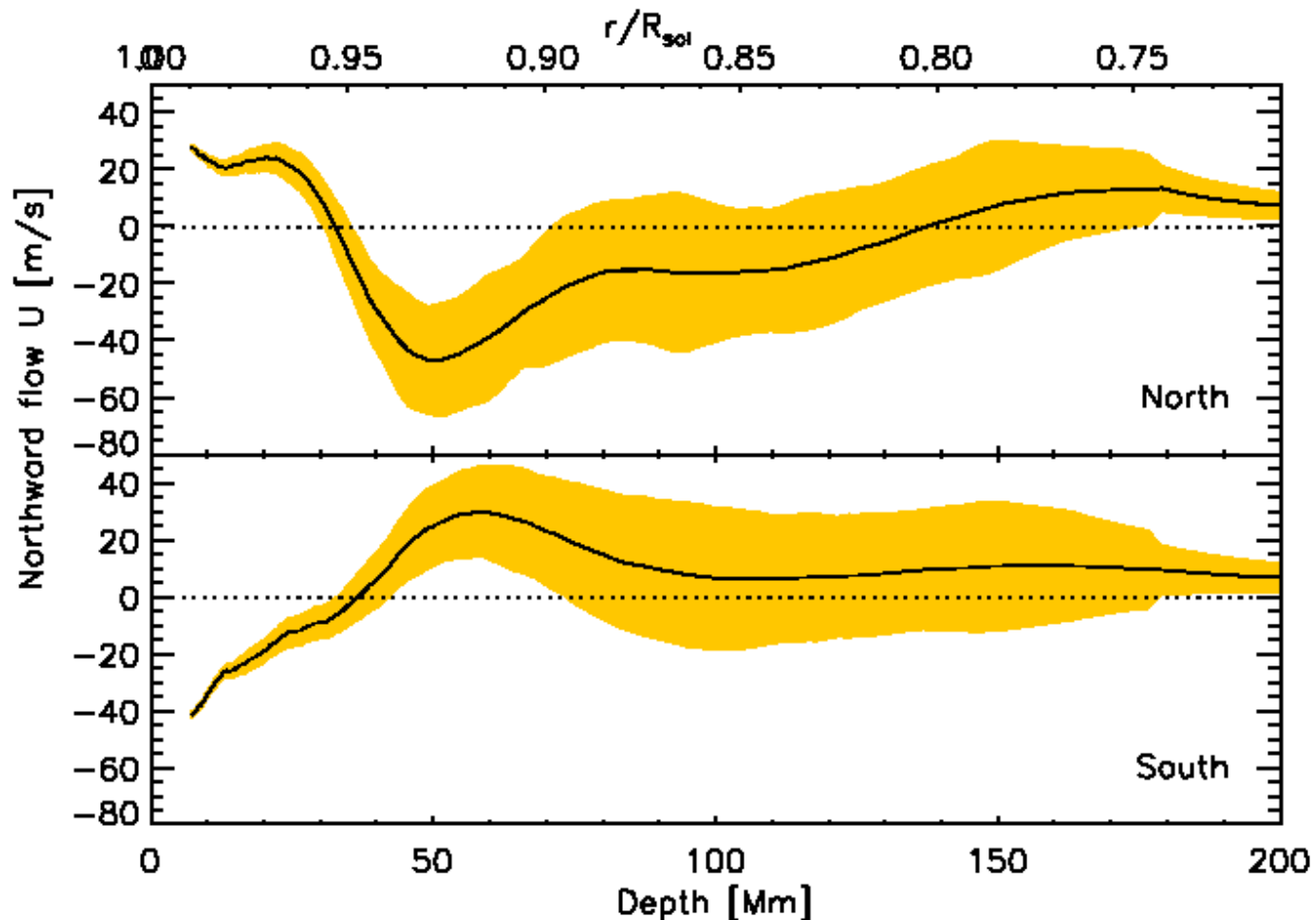
# Asymptotic inversion

(Christensen-Dalsgaard et al. 1990)

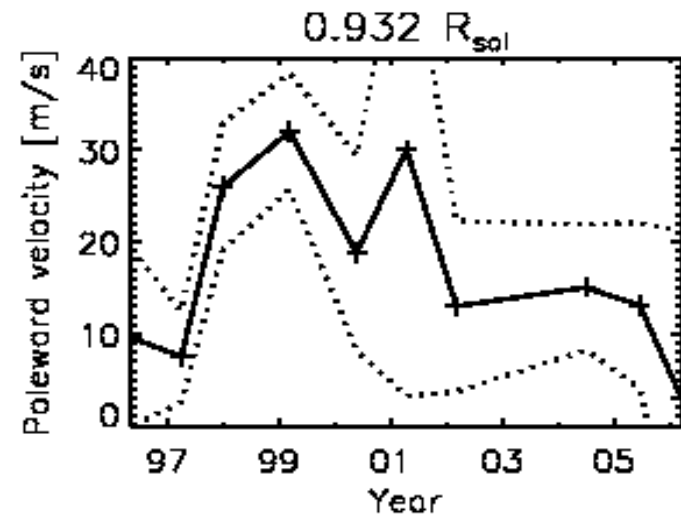
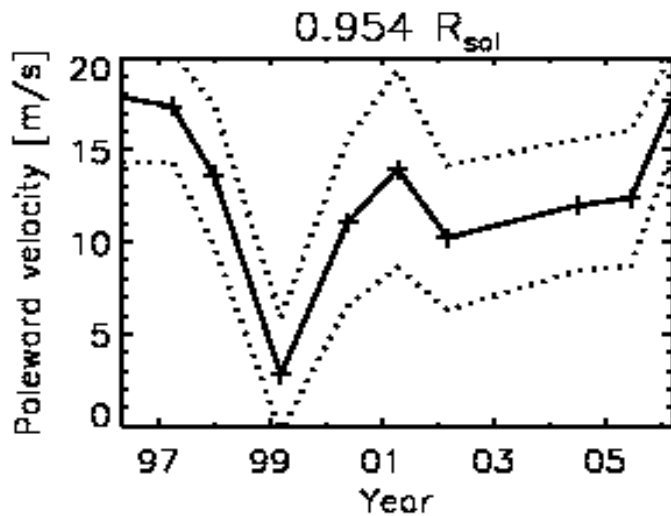
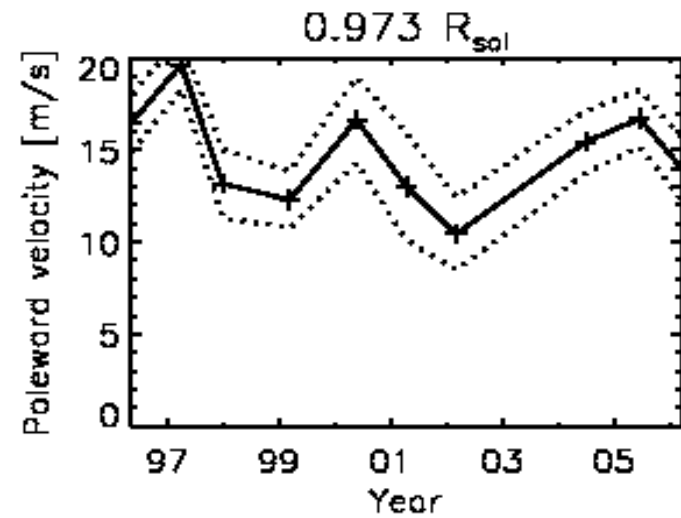
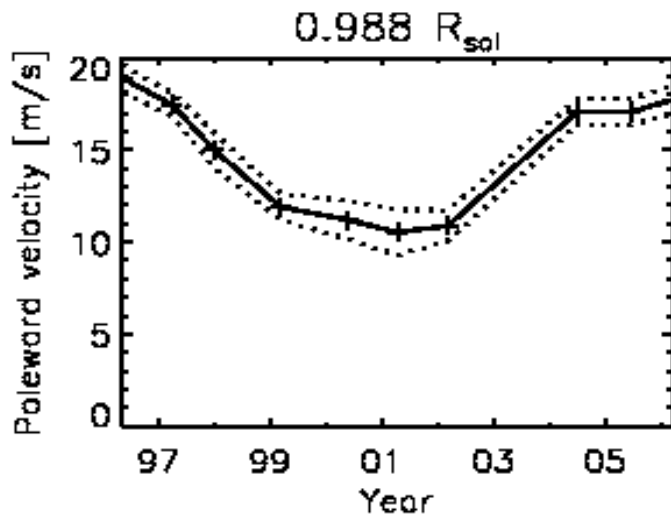
$$U(r) = \frac{-2a(r)}{\pi} \frac{d}{d \ln r} \int_{a(R_{\odot})}^{a(r)} \sqrt{\frac{1}{a^2(r) - w^2}} D(w) dw$$

- With radial coordinate  $r$
- flow profile  $U(r)$
- $a(r) := c(r)/r \quad w = 2\pi\nu/l.$
- $c(r)$  sound speed profile given by ModelS (Christensen-Dalsgaard et al. 1989, see also Sekii & Shibahashi 1989)
- $D(w) = U'(w)$  (“measured” velocity)

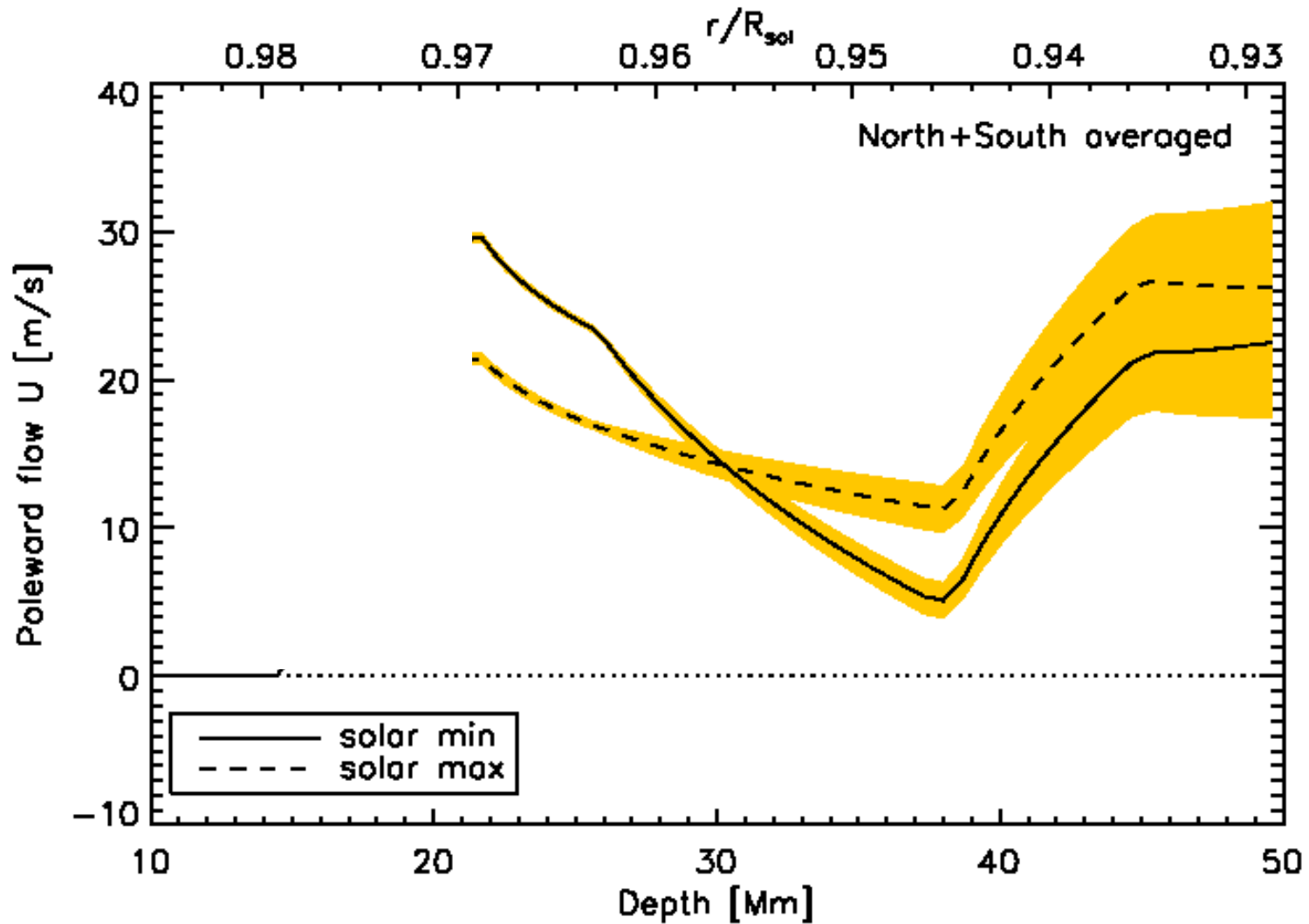
# Average 80 days inversion result during solar minimum



# Variations with the solar cycle

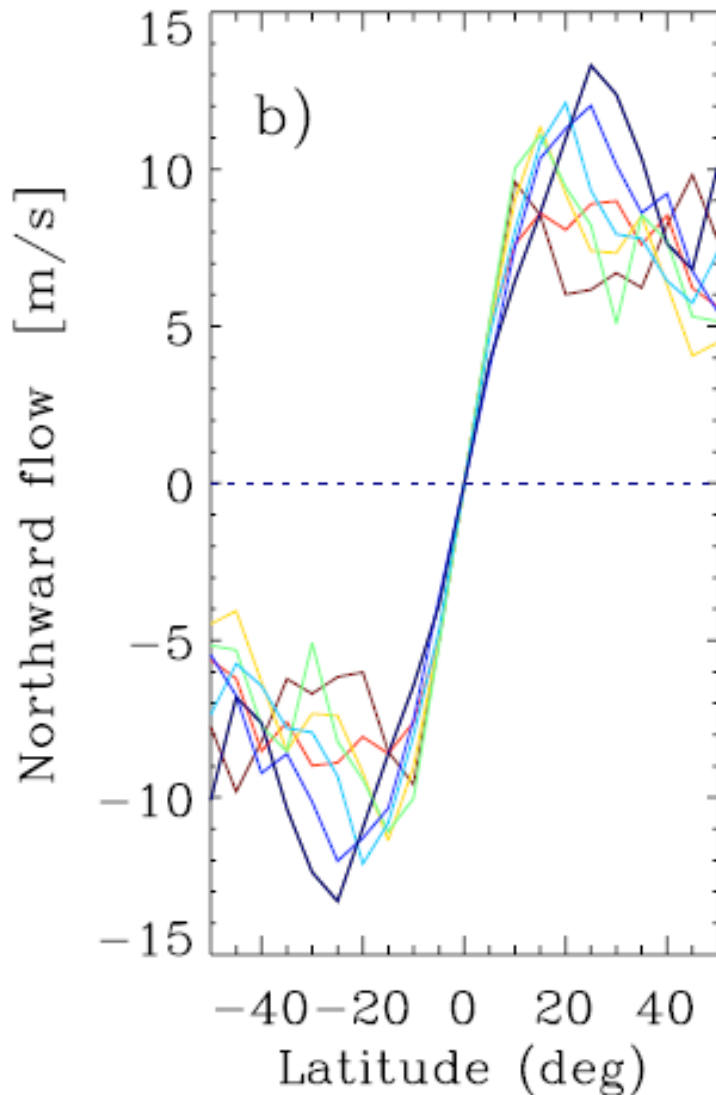


# Inversion result of solar min vs max



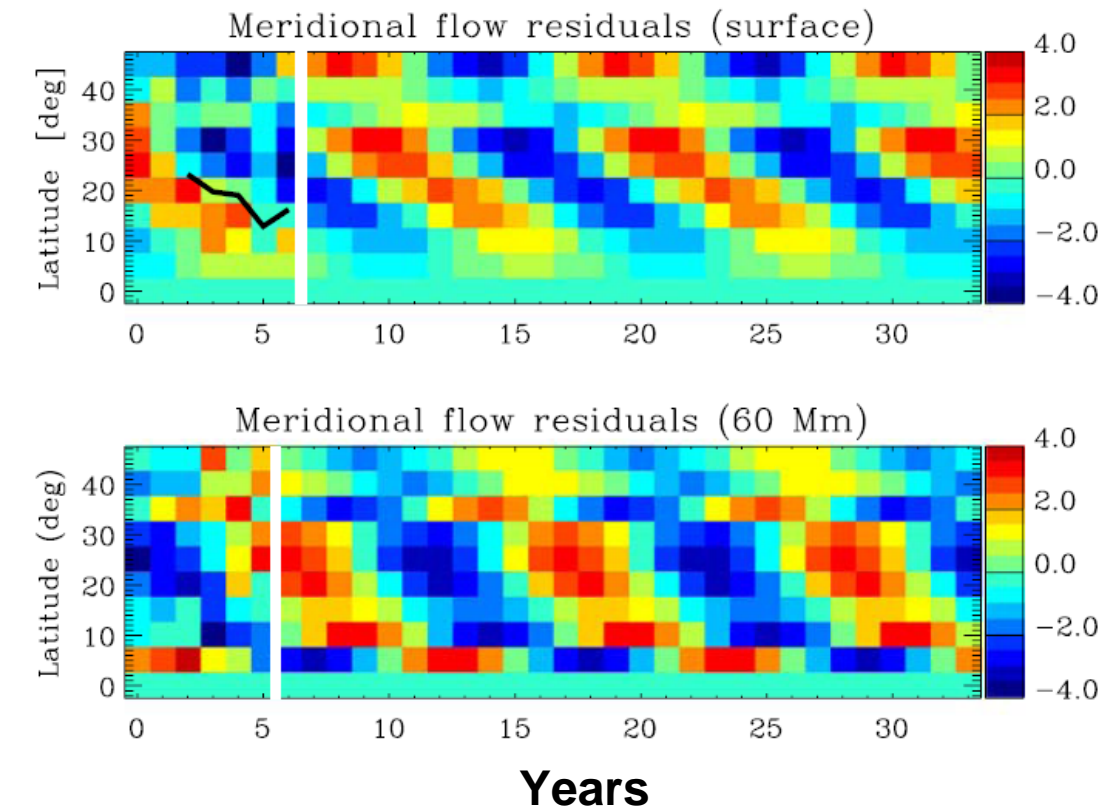
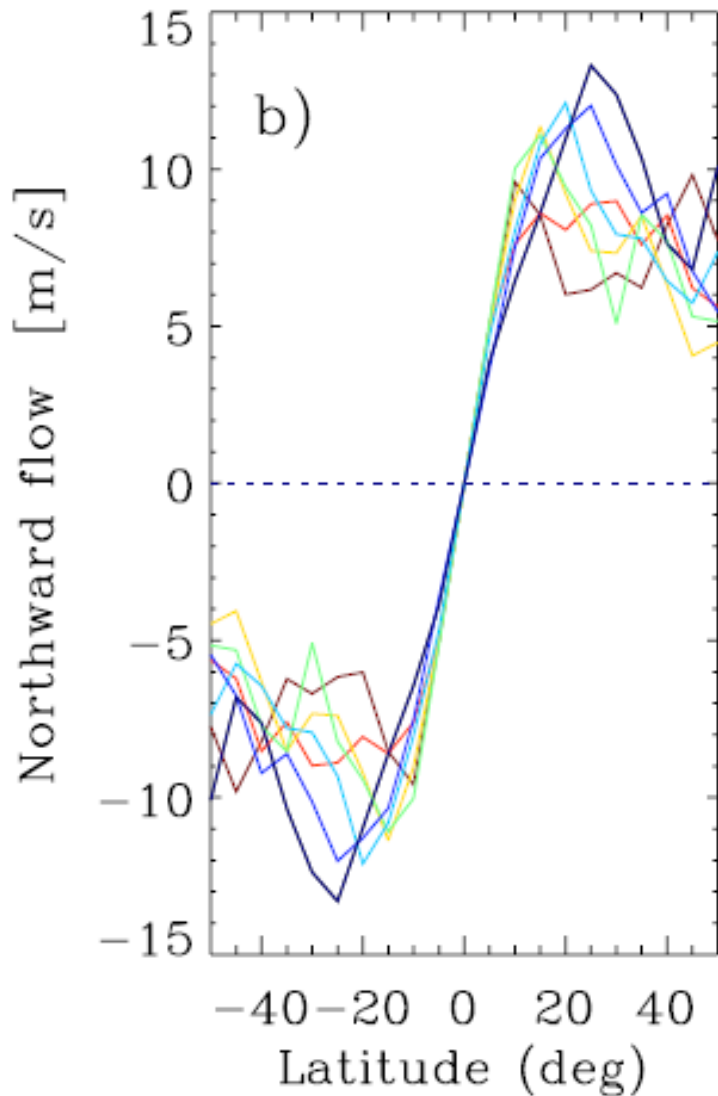


# Comparisons with other recent results

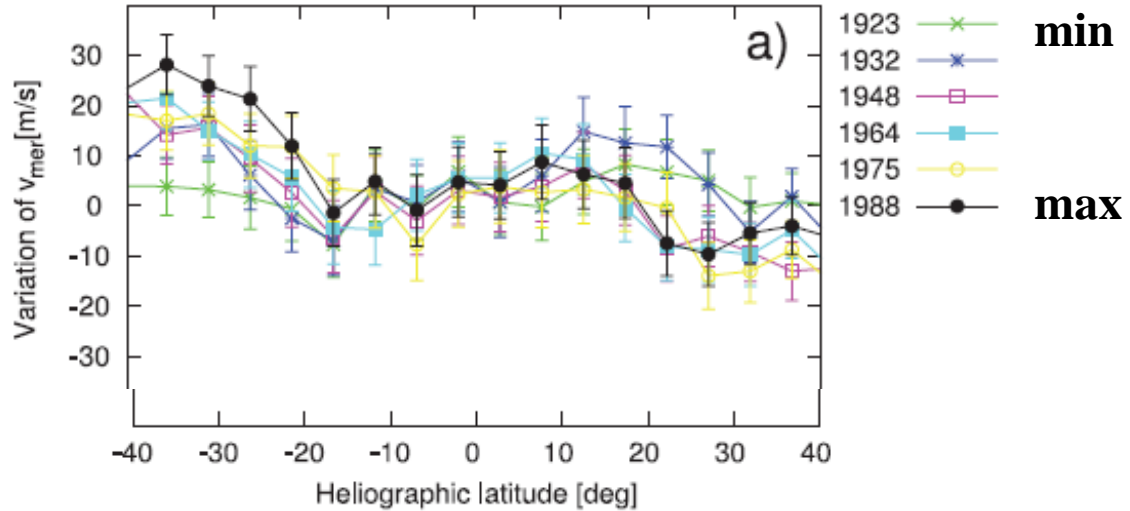
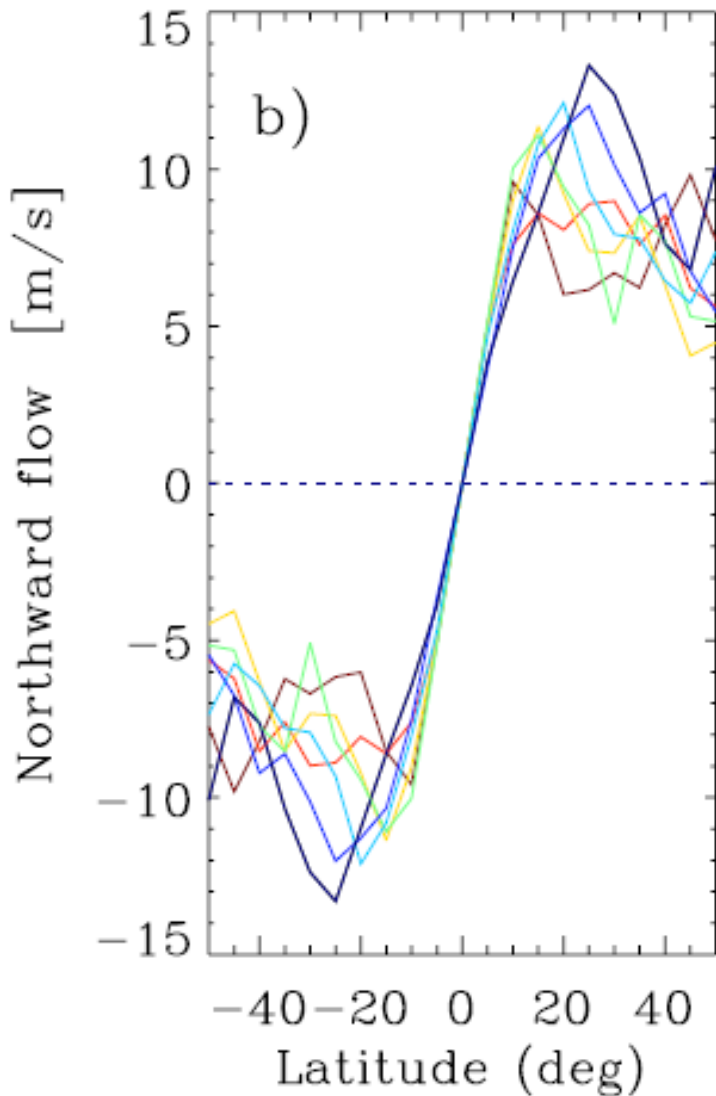


- Meridional flow near solar surface:
- From solar min in 1996 (blue) to solar max in 2002 (red)

# Comparisons with other recent results



# Comparisons with other recent results



Svanda, Kosovichev, Zhao (2008) ApJ **680** L161

# Conclusions

- For quiet Sun, find return flow at a depth of around 40 Mm -> Possibly two flow cells lying on top of each other
- Found variations with the solar cycle
  - Near-surface flow decreases from 20m/s to 10m/s, while the flow at deeper layers increases from solar min to solar max